

1 **Safety Ranking of Rural Curves Based on Design Consistency**  
2 **Measures**

3

4 **Jiří Ambros\***

5 Centrum dopravního výzkumu, v.v.i.

6 Líšeňská 33a, 636 00 Brno, Czech Republic

7 Tel: +420 541 641 362; Fax: +420 541 641 711; Email: jiri.ambros@cdv.cz

8

9 **Veronika Valentová**

10 Centrum dopravního výzkumu, v.v.i.

11 Líšeňská 33a, 636 00 Brno, Czech Republic

12 Tel: +420 541 641 355; Fax: +420 541 641 711; Email: veronika.valentova@cdv.cz

13

14 **Peter Oríšek**

15 Centrum dopravního výzkumu, v.v.i.

16 Líšeňská 33a, 636 00 Brno, Czech Republic

17 Tel: +420 541 641 355; Fax: +420 541 641 711; Email: peter.orisek@cdv.cz

18

19 \* Corresponding Author

20

21 Word count: 3,902 words of text + 6 figures × 250 words = 5,402 words

22

23 Submission Date: March 20, 2015

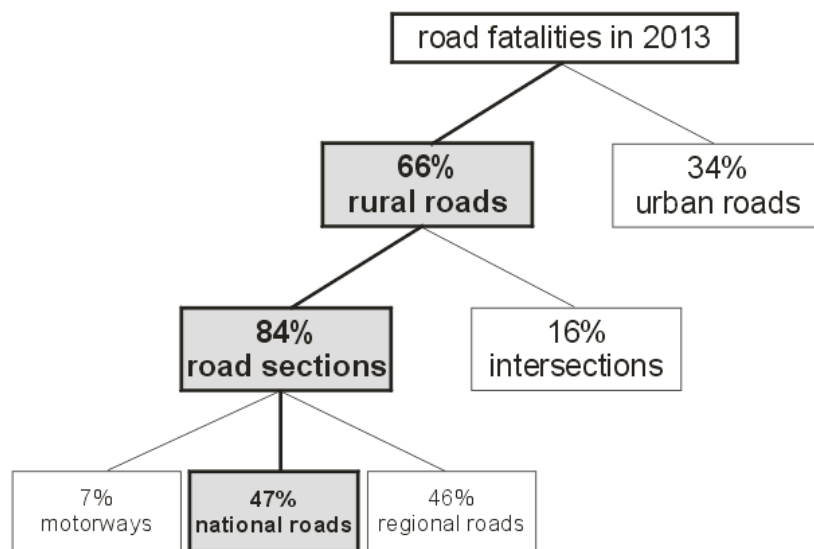
**1 ABSTRACT**

2 Speeding as a consequence of improper horizontal alignment of rural roads is one of current traffic  
3 safety issues on Czech roads. The evaluation of design consistency, i.e. a degree to which a road is  
4 designed and constructed to avoid critical driving manoeuvres, has been known as one of the  
5 promising tools in this regards. The objective of the presented study is to prove a practical  
6 application of this concept on a sample of Czech national road network without its design data. A  
7 data collection vehicle was used to obtain position data on selected roads. The data processing  
8 included a determination of horizontal alignment elements and segmentation and a calculation of  
9 consistency measures. The calculated speed consistency level allowed safety ranking of curves.  
10 These results are subsequently validated with the ranking based on crash frequency. At the end,  
11 several practical applications are outlined.

12 **Keywords:** alignment, curve, speed, design consistency, safety ranking

## 1 INTRODUCTION

Road horizontal alignment is one of general features which have a significant impact on driving and safety. It consists of tangents (straight sections) connected by horizontal curves and other transition elements. Curves are places of special interest for their higher crash risk due to additional centripetal forces exerted on a vehicle, driver expectations, and other factors (1). According to PIARC's Road Safety Manual (2), 25 to 30% of all fatal crashes world-wide occur on curves. This amount is even higher in the Czech Republic. According to the statistical year-books of Czech Traffic Police, more than one third of total road fatalities are related to curve crashes. In order to structure these numbers, disaggregated Police data were used for Figure 1. It provides a division of Czech road fatalities counts by road settings (rural or urban roads), road network elements (sections or intersections) and their categories: motorways, national roads (1<sup>st</sup> class roads) or regional roads (2<sup>nd</sup> and 3<sup>rd</sup> class roads).



13

14 **FIGURE 1 Division of Czech road fatalities counts by road settings according to 2013 police**  
15 **data.**

16 Each level of graph provides several blocks describes in terms of percentages of road fatalities in  
17 2013. The blocks with higher percentage in each level present more critical settings. For example,  
18 the first level documents that 66% of road fatalities occurred on rural roads, while remaining 34%  
19 occurred on urban roads; therefore, rural roads are more critical. Bold lines and grey blocks in  
20 Figure 1 illustrate the most critical settings through the whole graph: they are rural sections of  
21 national roads. In this category, approximately 40% of fatalities are related to curve crashes.  
22 Within these crashes on national roads speeding was attributed as the main cause of almost 40% of  
23 fatalities.

24 To sum up, this critical situation is to a great extent related to speeding consequences  
25 related to rural road curves. One of the reasons may be the lack of design consistency: drivers are  
26 likely to make fewer errors in the vicinity of geometric features that conform to their expectations  
27 than they do in the vicinity of features that violate their expectations (3). Consistent design should

1 ensure that successive geometric elements are coordinated in a manner that minimizes variability  
2 in vehicle speeds, prevents critical driving maneuvers and reduces crash risk (4, 5). Design  
3 consistency evaluation and improvement is therefore one of several promising tools that may be  
4 employed to improve roadway safety performance (6).

5 The objective of the presented study is to prove practical application of this concept on  
6 rural sections of the selected Czech national roads, without their design data. A data collection  
7 vehicle was used to obtain position data on the selected road network. The data processing  
8 included a determination of horizontal alignment elements and segmentation and calculation of  
9 design consistency measures. The calculated speed consistency level allowed safety ranking of  
10 curves. These results were subsequently validated with actual safety performance using the  
11 potential for safety improvement calculated with a crash prediction model and empirical Bayes  
12 method.

13 After this introduction and the following literature review the study is presented: firstly the  
14 data collection and analysis method is introduced, followed by results, and finished with  
15 discussion and conclusions.

16

## 17 **2 LITERATURE REVIEW**

18 Since one of the symptoms of a geometric feature that violates driver's expectation is inconsistent  
19 operating speed in the vicinity of this feature, consistent operating speeds are thought to be a  
20 product of consistent design (3). Therefore, variables for evaluating design consistency are usually  
21 defined in terms of operating speed (7).

22 McFadden and Elefteriadou (4) used 85<sup>th</sup> percentile of maximum speed reduction  
23 calculated from data in nine points on the curve and the approaching tangent; subsequently,  
24 Misaghi and Hassan (8) introduced 85<sup>th</sup> percentile speed reduction for individual drivers based on  
25 data from two points on the approaching tangent and at the middle of the curve. Cafiso et al. (9)  
26 used the following consistency measures in prediction modelling: a relative area bounded by the  
27 speed profile, a standard deviation of operating speed profile, average speed differential and speed  
28 differentials density. Camacho-Torregrosa et al. (10) developed an index based on speed  
29 differential and average speed reduction.

30 Nevertheless, one consistency measure has been used the most (6, 7, 9): based on the key  
31 works of Lamm and colleagues, design consistency is evaluated in terms of the magnitude of speed  
32 reduction between successive design elements. Design is regarded as 'good' if the magnitude of  
33 the difference in 85<sup>th</sup> percentile is lower than 10 km/h; the design is 'fair' if the difference is  
34 between 10 km/h and 20 km/h; and the design is 'poor' if the difference is higher than 20 km/h (11,  
35 12, 13).

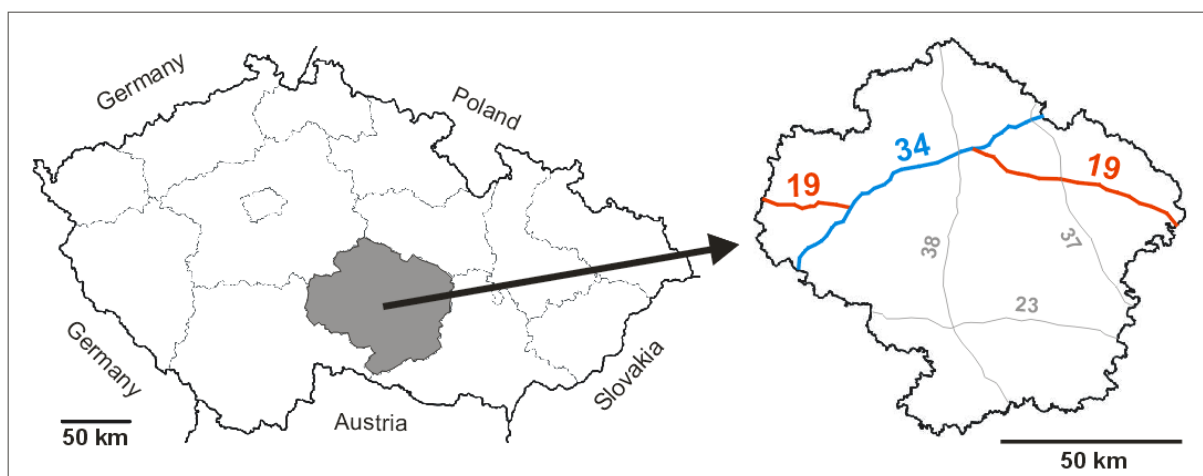
36 Should these measures be used, position and curvature data (horizontal alignment) have to  
37 be obtained. They may certainly be retrieved from map sources or project documentations.  
38 However, there may also be cases when the alignment parameters are unknown. GPS positioning  
39 has recently been used in this regards, followed by different approaches to segmentation and  
40 calculation of required measures (14 – 17).

1 In order to prove validity of safety ranking based on design consistency measures, a  
 2 comparison with crash situation is typically conducted. However, there are different approaches to  
 3 quantification of safety based on crash occurrences: while earlier studies used crash rates (e.g. 11,  
 4 18), other methods were recommended later, in order to take into account statistical characteristics  
 5 of crash data (e.g. 3, 19). Further differences are in the selection process of target group of crashes  
 6 believed to be related to road alignment: e.g. Anderson et al. (3) used both single- and  
 7 multi-vehicle crashes but excluded, among others, crashes with animals; on the other hand, Lamm  
 8 et al. (12) report that German comparison studies rely on run-off-the-road crashes and deer  
 9 crashes. Weller (20) saw 'driving' crashes (i.e. single vehicle crashes) as the only reasonable  
 10 category, while Turner et al. (21) combined loss-of-control and head-on crashes. Most authors do  
 11 not detail these considerations and use all the crashes together.

12

### 13 3 DATA COLLECTION AND ANALYSIS

14 The study was conducted in one of the Czech regions (Kraj Vysočina) with rolling terrain. There  
 15 are 5 national roads in this region; the ones with the highest traffic volumes and risk were selected  
 16 for the study (roads No. 19 and 34). Figure 2 shows where the region and the selected roads are  
 17 located. Both roads have an overlapping part which was considered as a part of road 34, as  
 18 indicated by colors in Fig. 2.



19

20 **FIGURE 2 Geographical location of selected national roads within the region and the Czech**  
 21 **Republic (<http://commons.wikimedia.org/>).**

22 The roads are paved, two-lane, undivided, approximately 7 meters wide. Approximate  
 23 average annual daily traffic volume is between 5,000 and 10,000 vehicles, general speed limit is 90  
 24 km/h. Figure 3 provides two illustrative photographs of selected roads. After excluding the road  
 25 sections in built-up areas (through-roads), their total length was approximately 100 km.



1

2 **FIGURE 3** Illustration of road environment on selected roads (<https://maps.google.cz/>).

3

4 **3.1 Alignment data**

5 The roads in question were driven through on two weekdays in November 2013, in one direction,  
6 as close as possible to free-flow speed. The inspection vehicle of Centrum dopravního výzkumu,  
7 v.v.i. (Transport Research Centre) was used for this purpose. It is a customized Volkswagen  
8 Transporter T5 vehicle instrumented with several position sensors (gyroscope, accelerometer,  
9 odometer) as well as controller area network (CAN) bus, whose data are synchronized and  
10 positioned using a precise GPS with the frequency of 10 Hz (10 records per second). At the typical  
11 speed of 90 km/h the speed synchronization period equals to 2.5 m of driven distance. All data  
12 were stored on a solid-state drive (SSD) in XML format.

13 It is difficult in the Czech Republic to obtain periodically updated and precise road design  
14 plans. Thus a method had to be developed in order to obtain alignment parameters and conduct  
15 segmentation into tangents and curves. The development and the pilot (non-automated)  
16 application of the methodology is described elsewhere (17); for this study it was programmed into  
17 an internal web module in order to ensure its wider application. It was developed using a PHP  
18 programming language and MySQL database system. The employed calculation procedure  
19 consisted of several steps:

- 20 – Transformation of data points into the Czech planar coordinate system JTSK.
- 21 – Calculation of distances and angles between points in order to calculate radii and lengths for  
22 each three consecutive points.
- 23 – Calculation of curvature change rate (CCR).
- 24 – Segmentation of data points into tangent and curve sections using CCR threshold; based on  
25 several tests, its value was set at 80 gon/km.

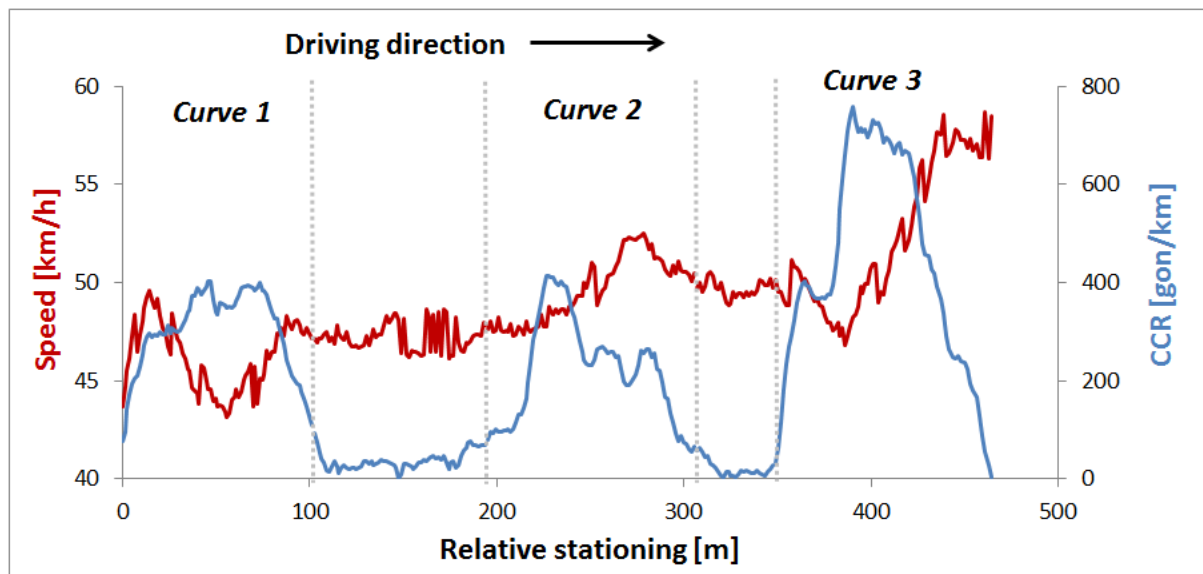
26 Details may be found in the paper describing the pilot study (17). The results of  
27 segmentation were visualized with HTML and JavaScript environment using MapQuest free  
28 online web mapping service. Figure 4 presents one example (grey dots form tangents, red dots are  
29 curves).



1

2 **FIGURE 4 Illustration of segmentation results (tangents in grey, curves in red).**

3 In terms of design consistency, each segment may be characterized by its values of CCR  
 4 and speed. These measures change continuously within a segment, as illustrated in Figure 5, which  
 5 shows the values related to the example section from Figure 4.



6

7 **FIGURE 5 Speed and curvature change rate (CCR) within road section from Figure 4.**

8 For each segment 85<sup>th</sup> percentile and average of CCR and speed were determined. The  
 9 presented study evaluated only curves. The CCR and speed values were used in the following steps  
 10 (crash modeling and validation).

11

### 12 3.2 Crash data

13 Crash locations are routinely georeferenced by Czech Traffic Police and described according to  
 14 their methodology. This information was used in the study with the following characteristics:

- 15 – 5-year period (2009 – 2013)
- 16 – All severity levels (property damage only, slight/severe/fatal injury)
- 17 – Only single-vehicle crashes

1 Using this definition, crashes on selected roads were retrieved from the Police database and  
 2 assigned as a crash frequency to each curve in QGIS software environment. As a risk exposure  
 3 indicator, traffic volume data were retrieved from the National Traffic Census data of the Czech  
 4 Road and Motorway Directorate.

5 In order to determine actual safety performance of each curve, an indicator of a potential  
 6 for safety improvement (PSI, see e.g. 22) was chosen. Its calculation required an estimation of  
 7 expected crash frequency using a crash prediction model and adjustment according to empirical  
 8 Bayes methodology. The crash prediction model was developed as a negative binomial regression  
 9 model with explanatory variables of traffic volume, average curvature and curve length in the  
 10 following form (for each curve  $i$ ):

$$11 \quad P_i = a \cdot AADT_i^b \cdot CCR_i^c \cdot \exp(d \cdot L_i) \quad (1)$$

12 where:

- 13  $P_i$  ... predicted (expected) crash frequency  
 14  $AADT_i$  ... annual average daily traffic volume  
 15  $CCR_i$  ... average curvature change rate  
 16  $L_i$  ... length  
 17  $a, b, c, d$  ... regression coefficients to be estimated

18 SPSS procedure GENLIN was used for the modeling. Consistently with the literature (see  
 19 e.g. 22, 23), further calculation steps for each curve  $i$  were as follows:

$$20 \quad EB_i = w_i \cdot P_i + (1 - w_i) \cdot R_i \quad (2)$$

$$21 \quad w_i = \frac{k_i}{k_i + P_i} \quad (3)$$

$$22 \quad k_i = k \cdot L_i \quad (4)$$

$$23 \quad PSI_i = EB_i - P_i \quad (5)$$

24 where:

- 25  $EB_i$  ... empirical Bayes estimate  
 26  $w_i$  ... weight  
 27  $P_i$  ... predicted crash frequency  
 28  $R_i$  ... recorded crash frequency  
 29  $k_i$  ... overdispersion parameter  
 30  $L_i$  ... curve length  
 31  $PSI_i$  ... potential for safety improvement

32

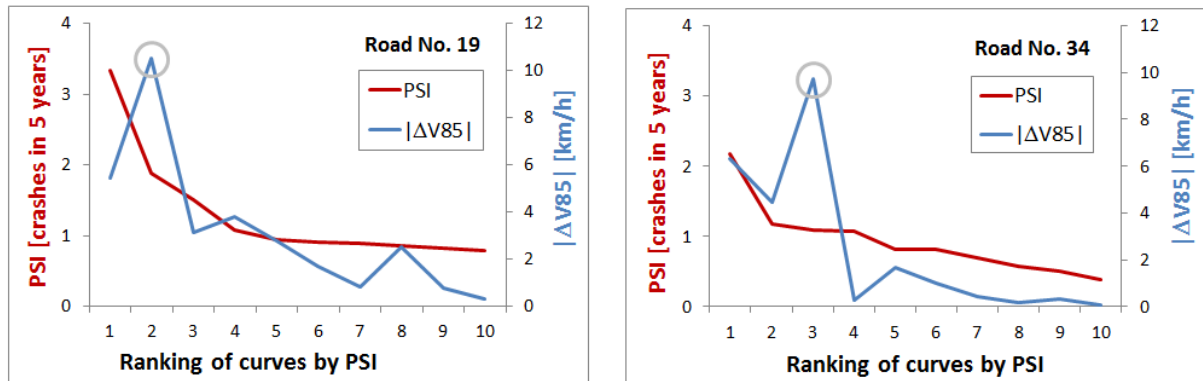
### 33 4 RESULTS

34 The objective of validation procedure was to compare the results of two rankings:

- 35 – potential for safety improvement (PSI) of curve  $i$  from the empirical Bayes method  
 36 – absolute difference of 85<sup>th</sup> percentile speeds ( $|\Delta V_{85}|$ ) between curve  $i$  and tangent  $i + 1$



1 Top ten curves ranked by descending PSI values (in units of crashes in 5 years) were used  
 2 in the following graphs (Fig. 6), separately for roads No. 19 and 34.



3  
 4 **FIGURE 6 Comparison of results for top ten curves according to ranking by potential for**  
 5 **safety improvement.**

6 In general, there is an obvious relationship between trends of PSI and  $|\Delta V_{85}|$ . However,  
 7 there is an outlying value of speed in both graphs (in grey circle). After checking specific locations  
 8 it was found that these were the curves where the vehicle was driving uphill.

9

## 10 5 DISCUSSION AND CONCLUSIONS

11 The objective of the presented study was to prove the practical application of design consistency  
 12 concept on rural sections of selected Czech national roads. The position data were collected by the  
 13 inspection vehicle and processed in order to obtain CCR necessary to distinguish the alignment  
 14 elements (tangents and curves). Speed consistency measure was calculated for each curve and  
 15 compared with its potential for safety improvement based on the crash prediction model and  
 16 empirical Bayes method. Both indicators were used in safety rankings of curves.

17 The results (Fig. 6) proved that there are relatively similar trends between both safety  
 18 rankings. However, outlying values were also detected – specifically in the curves with vertical  
 19 curvature which was not taken into account in the evaluation. There were also other limitations of  
 20 the presented study:

- 21 – *Data collection.* Data were collected within a single ride only and in a single driving direction.  
 22 Although there was an attempt to adapt driving speed to the free-flow as close as possible, the  
 23 collected data may not be representative of the driving population. In this regard, more drives,  
 24 possibly with more drivers, could offer more representative data, leading to different results.
- 25 – *Speed consistency measure.* Several studies recommended not to rely on a simple indicator of  
 26  $|\Delta V_{85}|$ , which was used in the presented study, since it may underestimate the real speed  
 27 reduction (4). Other measure, such as 85<sup>th</sup> percentile of maximum speed reduction, may  
 28 circumvent the issue (24).

- 1 – *Crash sample.* The sample of modeled crashes was generally small: 199 crashes occurred in  
2 total in curves of roads No. 19 and 34, of which only part (117) were single-vehicle crashes,  
3 used for the modeling. Samples should generally be larger, for example Jonsson (25)  
4 recommends at least 200 crashes in order to construct sound models. There is also a ‘low mean  
5 problem’: in the studied sample there is approximately 0.8 crash per curve, or 0.5  
6 single-vehicle crash per curve. This fact may produce unreliably estimated overdispersion  
7 parameter and therefore bias the following empirical Bayes estimate (26).  
8 – *Other influences.* There is certainly a number of factors which influenced both crash frequency  
9 and speed and were not controlled for in the presented study, e.g. vertical curvature, but also  
10 cross section parameters such as the number of lanes, road width and local speed restrictions.

11 Notwithstanding these limitations, the results showed that speed consistency is related to  
12 actual safety (in terms of potential for safety improvement) and may thus serve as a surrogate  
13 measure. Further research will aim at improving the evaluation methodology and enlarging the  
14 sample so that the results may be more representative and valid.

15 Once improved the method may have several practical applications in the future, some of  
16 which are described:

- 17 – *Identification of critical curves for efficient local reconstructions.* In Czech standards the  
18 process of road design is mostly dictated by the design speed, which is set according to road  
19 category. These standards not only govern new road design, but also reconstructions of current  
20 roads. During reconstructions it is often impossible to adhere to requirements of curve radii  
21 according to the design speed. The frequent reasons are larger property demands and  
22 subsequent higher construction costs. Therefore, frequently set lower design speed is applied  
23 in the whole road section, while the critical curve inconsistency itself remains untreated. The  
24 ranking method proposed in the paper would be beneficial for the identification of these local  
25 inconsistencies and thus directing the reconstruction efficiently.  
26 – *Proactive evaluation of selected roads.* Road agency may use the method to proactively  
27 evaluate selected roads, to compare or rank them, and to determine the importance of the  
28 application of road safety measures. A potential low-cost solution to improve road safety in the  
29 described locality and in some similar ones may then be immediately installed. The same holds  
30 for comprehensible road signing which would inform of the unsatisfactory curves. The  
31 consistent road signing would provide drivers with clear information about a situation they are  
32 to expect. This is important since Czech standards do not set a unified approach for installing  
33 suitable warning signs such as chevrons. These are often found at locations which are not as  
34 risky as others where such signs are missing. With the use of the mentioned method, the  
35 unsatisfactory curves could also be equipped with a road sign of advisory speed limit. It  
36 provides a useful way to inform drivers who do not drive through such route daily, while not  
37 limiting the drivers who are familiar with this route.  
38

## 1 ACKNOWLEDGMENTS

2 The authors would like to thank their colleagues Ondřej Gogolin for collecting data with the  
3 inspection vehicle and Jiří Sedoník for preparing crash data. The research was conducted with the  
4 support of the Czech Ministry of Education, Youth and Sports' research project No.  
5 CZ.1.05/2.1.00/03.0064 'Transport R&D Centre'.  
6

## 7 REFERENCES

- 8 1. Hummer, J. E., W. Rasdorf, D. J. Findley, C. V. Zegeer, and C. A. Sundstrom. Curve crashes:  
9 Road and collision characteristics and countermeasures. *Journal of Transportation Safety and*  
10 *Security*, Vol. 2, 2010, pp. 203–220.
- 11 2. *Road Safety Manual: Recommendations from the World Road Association (PIARC)*.  
12 Route2market, Harrogate, 2003.
- 13 3. Anderson, I. B., K. M. Bauer, D. W. Harwood, and K. Fitzpatrick. Relationship to Safety of  
14 Geometric Design Consistency Measures for Rural Two-Lane Highways. In *Transportation*  
15 *Research Record: Journal of the Transportation Research Board*, No. 1658, Transportation  
16 Research Board of the National Academies, Washington, D.C., 1999, pp. 43–51.
- 17 4. McFadden, J., and L. Elefteriadou. Evaluating horizontal alignment design consistency of  
18 two-lane rural highways: Development of new procedure. In *Transportation Research Record:*  
19 *Journal of the Transportation Research Board*, No. 1737, Transportation Research Board of  
20 the National Academies, Washington, D.C., 2000, pp. 9–17.
- 21 5. Fitzpatrick, K., and J. M. Collins. Speed-profile model for two-lane rural highways. In  
22 *Transportation Research Record: Journal of the Transportation Research Board*, No. 1737,  
23 Transportation Research Board of the National Academies, Washington, D.C., 2000, pp. 42–  
24 49.
- 25 6. Hassan, Y. Highway Design Consistency: Refining the State of Knowledge and Practice. In  
26 *Transportation Research Record: Journal of the Transportation Research Board*, No. 1881,  
27 Transportation Research Board of the National Academies, Washington, D.C., 2004, pp. 63–  
28 71.
- 29 7. Gibreel, G. M., S. M. Easa, Y. Hassan, and I. A. El-Dimeery. State of the Art of Highway  
30 Geometric Design Consistency. *Journal of Transportation Engineering*, Vol. 125, 1999, pp.  
31 305–313.
- 32 8. Misaghi, P., and Y. Hassan. Modeling Operating Speed and Speed Differential on Two-Lane  
33 Rural Roads. *Journal of Transportation Engineering*, Vol. 131, 2005, pp. 408–417.
- 34 9. Cafiso, S., A. Di Graziano, G. Di Silvestro, G. La Cava, and B. Persaud. Development of  
35 comprehensive accident models for two-lane rural highways using exposure, geometry,  
36 consistency and context variables. *Accident Analysis and Prevention*, Vol. 42, 2010, pp. 1072–  
37 1079.

- 1 10. Camacho-Torregrosa, F. J., A. M. Pérez-Zuriaga, J. M. Campoy-Ungría, and A.  
2 García-García. New geometric design consistency model based on operating speed profiles for  
3 road safety evaluation. *Accident Analysis and Prevention*, Vol. 61, 2013, pp. 33–42.
- 4 11. Lamm, R., B. Psarianos, and S. Cafiso. Safety Evaluation Process for Two-Lane Rural Roads:  
5 A 10-Year Review. In *Transportation Research Record: Journal of the Transportation*  
6 *Research Board*, No. 1796, Transportation Research Board of the National Academies,  
7 Washington, D.C., 2002, pp. 51–59.
- 8 12. Lamm, R., Psarianos, B., Mailänder, T. *Highway Design and Traffic Safety Engineering*  
9 *Handbook*. McGraw-Hill, Columbus, 1999.
- 10 13. Lamm, R., A. Beck, T. Ruscher, T. Mailänder, S. Cafiso, and G. La Cava. *How To Make*  
11 *Two-Lane Rural Roads Safer: Scientific Background and Guide for Practical Application*.  
12 WIT Press, Southampton, 2007.
- 13 14. Ben-Arieh, D., S. Chang, M. Rys, and G. Zhang. Geometric Modeling of Highways Using  
14 Global Positioning System Data and B-Spline Approximation. *Journal of Transportation*  
15 *Engineering*, Vol. 130, 2004, pp. 632–636.
- 16 15. Castro, M., L. Iglesias, R. Rodríguez-Solano, and J. A. Sánchez. Geometric modelling of  
17 highways using global positioning system (GPS) data and spline approximation.  
18 *Transportation Research Part C*, Vol. 14, 2006, pp. 233–243.
- 19 16. Biagioni, J., and J. Eriksson. Inferring Road Maps from Global Positioning System Traces:  
20 Survey and Comparative Evaluation. In *Transportation Research Record: Journal of the*  
21 *Transportation Research Board*, No. 2291, Transportation Research Board of the National  
22 Academies, Washington, D.C., 2012, pp. 61–71.
- 23 17. Ambros, J., and V. Valentová. Identification of road horizontal alignment inconsistencies – A  
24 pilot study from the Czech Republic. *The Baltic Journal of Road and Bridge Engineering*, in  
25 press.
- 26 18. Brenac, T. Safety at Curves and Road Geometry Standards in Some European Countries. In  
27 *Transportation Research Record: Journal of the Transportation Research Board*, No. 1523,  
28 Transportation Research Board of the National Academies, Washington, D.C., 1996, pp. 99–  
29 106.
- 30 19. Persaud, P., R. A. Retting, and C. Lyon. Guidelines for Identification of Hazardous Highway  
31 Curves. In *Transportation Research Record: Journal of the Transportation Research Board*,  
32 No. 1717, Transportation Research Board of the National Academies, Washington, D.C.,  
33 2000, pp. 14–18.
- 34 20. Weller, G. *The Psychology of Driving on Rural Roads: Development and Testing of a Model*.  
35 VS Verlag, Wiesbaden, 2010.
- 36 21. Turner, S., R. Singh, R., and G. Nates. *The next generation of rural road crash prediction*  
37 *models: final report*. NZ Transport Agency research report 509. NZTA, Wellington, 2012.

- 1 22. Persaud, B., C. Lyon, and T. Nguyen. Empirical Bayes Procedure for Ranking Sites for Safety  
2 Investigation by Potential for Safety Improvement. In *Transportation Research Record:  
3 Journal of the Transportation Research Board, No. 1665*, Transportation Research Board of  
4 the National Academies, Washington, D.C., 1999, pp. 7–12.
- 5 23. Hauer, E., D. W. Harwood, F. M. Council, and M. S. Griffith. Estimating Safety by the  
6 Empirical Bayes Method: A Tutorial. In *Transportation Research Record: Journal of the  
7 Transportation Research Board, No. 1784*, Transportation Research Board of the National  
8 Academies, Washington, D.C., 2002, pp. 126–131.
- 9 24. Park, Y., and F. Saccomanno. Evaluating speed consistency between successive elements of a  
10 two-lane rural highway. *Transportation Research Part A*, Vol. 40, 2006, pp. 375–385.
- 11 25. Jonsson, T. *Predictive models for accidents on urban links: A focus on vulnerable road users.*  
12 Bulletin 226. Lund University, Lund, 2005.
- 13 26. Lord, D. Modeling motor vehicle crashes using Poisson-gamma models: Examining the effects  
14 of low sample mean values and small sample size on the estimation of the fixed dispersion  
15 parameter. *Accident Analysis and Prevention*, Vol. 38, 2006, pp. 751–766.